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The pressure dependence of the structure and superconducting transition temperature of MgB₂

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Abstract

We have developed the potential parameters for the simulation of MgB₂ and calculated the variations of lattice parameters and volume with pressure up to 240 GPa. Our calculated results are in good agreement with experimental results below 40 GPa. By employing the McMillan expression, it is found that the lattice stiffening dominates the behaviour of the superconducting transition T_c under pressure in the scope of BCS theory. Using our calculated Grüneisen parameter γ_G , the simulated pressure effect on T_c accords well with experimental results. Our result shows that the T_c of MgB₂ can be destroyed by high pressure.

(Some figures in this article are in colour only in the electronic version)

1. Introduction

The recent discovery of superconductivity in MgB₂ [1], which has a high critical temperature T_c of about 40 K, has initiated a lot of interest. MgB₂ exhibits an AlB₂-type hexagonal structure, with a = 3.084 Å, c = 3.522 Å [2], space group P6/mmm. Soon after the discovery of MgB₂, many experimental studies were reported on tunnelling [3], specific-heat measurement [4, 5], isotope effect [6, 7] and inelastic neutron scattering measurements of the phonon density of states [8]. All of these works have tried to understand the mechanism of superconductivity.

Pressure is an important variable as it can be used to test the validity of some theoretical models. A large value of dT_c/dP may indicate that a higher value of T_c can be obtained by chemical means. To our knowledge, all high-pressure studies on MgB₂ show that T_c decreases with pressure, but the values of the pressure derivative dT_c/dP are quite different. Monteverde *et al* [9] and Lorenz *et al* [10] found that MgB₂ has an initial dT_c/dP of -0.8 and -1.6 K GPa⁻¹, respectively. Saito *et al* [11] reported a somewhat larger dT_c/dP of -2.0 K GPa⁻¹ from high-pressure resistivity measurements. By using an He-gas apparatus, Tomita *et al* [12] obtained a dT_c/dP of -1.11 K GPa⁻¹ under pure hydrostatic pressure

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conditions. Deemyad *et al* [13] suggested that all these different values of dT_c/dP reported may result primarily from shear-stress effects in nonhydrostatic pressure media rather than from the differences in the samples, and $dT_c/dP = -1.1$ K GPa⁻¹ should be the true hydrostatic pressure dependence of T_c in MgB₂.

Two theoretical models were proposed to describe the systematics of the pressure effect on T_c in MgB₂. Based on the theory of hole superconductivity, Hirsch [14] predicted a positive pressure effect on T_c . However, this prediction has not been confirmed by experiments. On the contrary, analysing the experimental results [12, 15] in terms of the McMillan expression [16] derived from Eliashberg theory [17] supports the theory that MgB₂ is an electron–phonon mediated superconductor.

Up to date, there has been no report about a pressure-induced structural transition of MgB_2 up to 40 GPa [18], and the superconductivity is not destroyed up to 44 GPa where T_c is still as high as 12 K [19]. Much higher pressure may be necessary to test whether pressure can cause a structural transition or finally destroy the superconductivity.

In this paper, we developed the potentials for calculation of MgB₂ through a GULP program [23], and with these potentials, we calculated the variations of lattice parameters and volume with pressure up to 240 GPa by using a PARAPOCS program [21]. Employing the McMillan expression and following the analysis of Chen *et al* [20], we investigated the pressure dependence of T_c of MgB₂.

2. Computational method

The crystal structure of a material at a given temperature and pressure can be predicted by minimizing its free energy. Our approach is to adjust the cell volume and atomic positions until the net pressure or stress is zero. The pressure P is simply the derivative of the free energy F with respect to volume V. Thus for a cubic material,

$$P = \mathrm{d}F/\mathrm{d}V.\tag{1}$$

Calculating the free energy at a given volume and then recalculating it after making a small adjustment to the cell volume dV determines the pressure. The problem becomes slightly more complicated for non-cubic material, as the volume will not expand isotropically. For these systems we have to consider six different strain components, ε_j . However, the same approach is used except that a small strain is applied in each of the six senses, and a pressure corresponding to the derivative of the free energy for each component is calculated assuming that the thermal contribution to the pressure is isotropic:

$$P_j = \frac{1}{V} \frac{\mathrm{d}F}{\mathrm{d}\varepsilon_j} \tag{2}$$

where V is the unit cell volume. During the iterative procedure a constant volume energy minimization is performed. Hence each time the cell volume is modified, all atomic positions are adjusted so that they remain at a potential energy minimum. Thus by minimizing to constant pressure and including the vibrational component of the free energy, the crystal structure at a given temperature and pressure can be predicted. This technique has been successfully used for simulation of many kinds of materials. Details of this technique are available in [21, 22].

Our simulation is based on the widely used and highly successful shell model generalization of the Born model of a solid. Short-range interaction forces are represented by a Buckingham potential:

$$V(r) = A \exp(-r/\rho) - Cr^{-6}$$
(3)

(a) Short-range interaction	A (eV)	ρ (Å)	$C \text{ (eV Å}^6)$
Mg ²⁺ -B ¹⁻	86.9086	0.600 902	0.0000
$B^{1-}-B^{1-}$	79 557.5217	0.180 512	285.2026
$Mg^{2+}-Mg^{2+}$	500.0000	0.406 700	0.0000
(b) Shell model parameters			
Species	Y (e)	K (eV Å ⁻²)	
Mg ^{2+ a}	0.420	349.95	

 Table 1. Potential parameters for MgB₂: short-range interaction and shell model parameters.

а	Reference	[23]	
	KULUIUUU	140	•

Table 2. Comparison of calculated and experimental structural data for MgB₂.

	Experimental ^a	Calculated	Difference
Lattice parameters (Å)			
а	3.084	3.0839	0.003 24%
С	3.522	3.5219	0.00284%
Bond lengths (Å)			
Mg–Mg	3.084	3.0839	0.0001 Å
Mg–B	2.504	2.5043	0.0003 Å
B–B	1.781	1.7805	0.0005 Å

^a Reference [2].

where A, ρ , and C are constants. For MgB₂, the charge states of 2+ and 1– are assigned to Mg and B, respectively. The potential parameters for MgB₂ are obtained by an empirical method (known as the 'relaxed' fitting approach), the structure is relaxed to zero strain for every evaluation of the sum of squares, and the difference between observed and calculated structural parameters is used in place of the derivatives. In each step in the fitting the minimization was started from the experimental structure to avoid the possibility that the fit becomes trapped in an undesirable local minimum in either potential of geometry space. It should be stressed that the reliability of the simulations depends on the validity of the potential model used in the calculation, and the latter is assessed primarily by its ability to reproduce experimental crystal properties. The potential parameters used in this work are given in table 1. The comparison of calculated and the experimental data is shown in table 2. The differences in lattice parameters and bond lengths between the calculated and experimental data are very small.

3. Results and discussion

Figure 1 shows the comparison of calculated lattice parameters *a* and *c* with the experimental data [18, 24, 25] up to 40 GPa. The calculated data agree well with the experimental data [18, 24, 25] below 10 GPa. The derivative of lattice parameter *a* (d*a*/d*P*) is -4.5×10^{-3} Å GPa⁻¹ up to 10 GPa. At 40 GPa our calculated lattice parameter *a* is 2.97 Å, which is 0.68% larger than the experimental value [18]. The variation of calculated lattice parameter *c* with pressure below 10 GPa also agrees well with the experimental data [18, 24, 25]. The derivative of lattice parameter *c* (d*c*/d*P*) is -9.2×10^{-3} Å GPa⁻¹ up to 10 GPa, which is twice as large as d*a*/d*P*. As the pressure increases to 40 GPa, our result also accords well with high-pressure experimental data. At 40 GPa our calculated value of *c* is 3.21 Å, which is 0.63% larger than the experimental value [18]. These results show that our calculated lattice parameters are in good agreement with experimental data up to 40 GPa. We find that there is



Figure 1. The calculated variation of lattice parameters of MgB_2 with pressure compared with experimental data up to 10 GPa. The inset shows the calculated lattice parameters up to 40 GPa. (a) The variation of lattice parameter *a* with pressure. (b) The variation of lattice parameter *c* with pressure.



Figure 2. (a) Calculated variations of lattice parameters a and c of MgB₂ with pressure up to 240 GPa. (b) The calculated variation of c/a with pressure up to 240 GPa.

no phase transition below 40 GPa, and this result is also in agreement with the experimental result [18].

Figure 2(a) shows the variations of the lattice parameters a and c with pressure up to 240 GPa. It is found that lattice parameter c decreases almost linearly with pressure up to 200 GPa while lattice parameter a decreases monotonically, following a quadratic dependence on applied pressure up to 40 GPa. It is interesting that the two curves intersect at about 90 GPa. After this point, lattice parameter c becomes much smaller than a as the pressure increases.



Figure 3. The calculated variation of volume of MgB_2 with pressure up to 20 GPa compared with the experimental data. The inset shows the volume dependence on pressure up to 240 GPa.

We also find two cusps in each curve, which may correspond to two structural transition points: one is at 140 GPa and the other is at 200 GPa. Figure 2(b) shows that the ratio of c/a decreases with increasing pressure, following a quadratic dependence on pressure up to 180 GPa. The initial ratio of c/a is 1.142, which is similar to the value (c/a = 1.141) obtained by Jorgensen *et al* [26]. It is known that when pressure is applied, the AlB₂ structure tends to change to the UHg₂ structure [27]. AlB₂ and UHg₂ are isopointal structures, distinguished only by their c/a ratio, which are 0.95–1.20 and 0.60–0.85, respectively. MgB₂ is of the AlB₂ structure, so [27] predicts that MgB₂ may also change to the UHg₂ structure transition. Our MgB₂ high-pressure structure calculation show that the structure transition from AlB₂ structure to UHg₂ structure is possible (see figure 2(b)), and this result is in agreement with the result predicted by Loa *et al* [27].

Figure 3 shows the variation of the calculated volume of MgB₂ with pressure up to 240 GPa. Our calculated result agrees well with the experimental data [18, 25, 28, 29] below 10 GPa. At 40 GPa our calculated result of 24.48 Å³ is only 1.16% different from the experimental value [18]. The extracted value of the bulk modulus $B_0 = -\partial P/\partial \ln V$ from figure 3 is 170.2 GPa, which is in good agreement with the experimental value of 172 GPa [30]. All our calculated results (lattice parameters and volume) are in excellent agreement with the experimental results. This shows that our potentials are good and the calculated results are reliable. For a superconductor, the change of structure may contain valuable information on the superconducting mechanism itself. Studying the structure dependence of pressure, especially under high-pressure, may find some unusual properties and benefit theoretical research. In this aspect our results are a useful supplement to predict structural variations of MgB₂ under high pressure from 40 to 240 GPa, because no experimental data have been reported in this pressure range. The superconducting transition temperature T_c is a result of both the raising effect of anisotropy in the electron-phonon couplings and the lowering effect of anharmonicity in the relevant phonon modes [31]. If we want to study the superconducting transition temperature of MgB₂, a solution, which can be expressed by lattice parameters, of the fully anisotropic Eliashberg equations is needed. However, there is as yet no report on such a solution. So in this paper we employ the McMillan expression [18], which is a solution of the isotropic Eliashberg equations, to analyse the pressure effect on T_c . The McMillan expression is

$$T_{\rm c} = \frac{\langle \omega \rangle}{1.2} \exp\left[\frac{-1.04(1+\lambda)}{\lambda - (1+0.62\lambda)\mu^*}\right],\tag{4}$$

which connects the value of T_c with the electron-phonon coupling parameter λ , the logarithmically averaged phonon frequency $\langle \omega \rangle$, and the Coulomb repulsion μ^* .

From inelastic neutron studies [8] we obtained the parameters at ambient pressure: $\langle \omega_0 \rangle = 670$ K, $T_c = 39.2$ K and $\lambda_0 = 0.9$ by using the most frequently cited value of $\mu_0^* = 0.1$. Following the analysis of Chen *et al* [20], we set $\langle \varpi \rangle = \langle \varpi_0 \rangle (V/V_0)^{-\gamma_G}$, $\lambda = \lambda_0 (V/V_0)^{\varphi}$ and $\mu^* = \mu_0^* (V/V_0)^{\phi}$, where $\varphi = -0.1\gamma_G - 0.09\gamma_N + 6.7 \times 10^{-3}$ and $\phi = -\gamma_N - 0.67 + 2\gamma_G$. It is found that variations of the parameters $\langle \omega \rangle$, μ^* and λ with volume are only decided by two parameters: γ_N and the Grüneisen parameter γ_G . The former is defined as $\gamma_N = \partial \ln N(E_f)/\partial \ln V$, which represents an effect of the density of electronic states at the Fermi level, and the latter is defined as $\gamma_G = -\partial \ln(\varpi^2)^{1/2}/\partial \ln V$, which represents an effect of the lattice stiffening. The calculated values of γ_N in the literature are 0.46 [20] and 2/3 in the case of a free-electron gas, and the calculated Grüneisen parameter γ_G in the literature has values ranging from 1.0 to 3.7 [12, 13, 20, 32, 33] while the experimental value is 2.9 [24].

Using the calculated pressure dependence of volume for MgB₂, we studied how the lattice stiffening and the density of electronic states at the Fermi level affect T_c under pressure by varying γ_G and γ_N using the McMillan expression. Figure 4(a) shows our calculated pressure dependence of T_c with different values of γ_G for a fixed $\gamma_N = 0.46$. It is found that γ_G determines the magnitude and sign of dT_c/dP . When γ_G is 0.6, T_c increases with increasing pressure. When γ_G is in the range of 0.8–1.2, T_c decreases slowly with increasing pressure. When γ_G is larger than 1.6, T_c can be destroyed by pressure below 160 GPa. The larger the γ_G , the lower the critical pressure. This suggests that the lattice stiffening has a significant effect on T_c under pressure. Figure 4(b) shows the comparison of our calculated pressure dependence of T_c using different values of γ_G with the experimental data. We find that most experimental data correspond to the γ_G range of 1.6–3.7. However, this range is wider than has been reported [20].

Figure 5 shows how the density of electronic states at the Fermi level affects T_c with fixed γ_G values of 1.6 and 3.7. For a fixed γ_G , a smaller γ_N causes faster decrease of T_c with increasing pressure. The smaller the γ_G , the larger the effects of γ_N on T_c . Compared with figure 4(a), we find that γ_G plays a more important role on T_c than γ_N . We conclude that the lattice stiffening under pressure plays a more crucial role on T_c than the density of electronic states at the Fermi level.

Employing the expression of $\gamma_{\rm G} = -2/3 - (V \partial^2 P / \partial V^2)/(2\partial P / \partial V)$ [34], we calculated the Grüneisen parameter $\gamma_{\rm G} = 2.55$ at 0 GPa from our calculated pressure dependence of volume, which is in reasonable agreement with the value of 2.9 from Raman spectroscopy studies [24]. Using $\gamma_{\rm G} = 2.55$ calculated by us and $\gamma_{\rm N} = 0.46$ obtained by Chen *et al* [20], we calculated the pressure dependence of $T_{\rm c}$ (figure 6). The calculated result agrees well with the experimental data [9, 10, 12, 15, 35, 36] below 30 GPa. We obtain the initial pressure derivative $dT_{\rm c}/dP = -1.05$ K GPa⁻¹ which accords with the hydrostatic pressure results [10, 12, 13]. This indicates that our calculated Grüneisen parameter $\gamma_{\rm G}$ is reasonable



Figure 4. (a) The calculated effect of γ_G on the pressure dependence of T_c of MgB₂ with fixed $\gamma_N = 0.46$ up to 240 GPa. (b) The calculated effect of γ_G on the pressure dependence of T_c of MgB₂ with fixed $\gamma_N = 0.46$ up to 40 GPa compared with the experimental data.

and the curves shown in figure 6 can roughly describe the behaviour of T_c under pressure. Lacking high-pressure experimental data, researchers can only predict whether high pressure



Figure 5. The calculated effect of γ_N on the pressure dependence of T_c of MgB₂ with $\gamma_G = 1.6$ and 3.7.



Figure 6. The calculated variation of T_c with pressure in MgB₂ compared with the experimental data.



Figure 7. The calculated T_c of MgB₂ versus structure parameter (c/a).

will destroy the superconductivity by analysing the available low-pressure experimental data, in which T_c does still not reach zero. We can provide the pressure dependence of T_c in the high-pressure range. We find that T_c is destroyed at about 90 GPa (figure 6), which is larger than the predicted value of 75 GPa [35] and in agreement with 93 GPa predicted by Deemyad *et al* [13]. Our result supports the prediction that sufficiently high pressure may destroy the superconductivity [37, 38].

Among the four important phonon vibration modes (E_{1u} , A_{2u} , E_{2g} and B_{1g}) in MgB₂, the E_{2g} mode seems to be a crucial contribution to T_c and to have a close correlation with the in-plane B–B bond length. When the pressure increases from 0 to 90 GPa where T_c is almost zero, from our calculations of the pressure dependence of lattice parameters, we find that the in-plane B–B bond length drops from 1.78 to 1.67 Å, which is close to its optimal value of 1.65 Å. This interesting result suggests that the stretched in-plane B–B bond length at ambient pressure may result in a higher T_c . Combining the calculated results of c/a and T_c , we plot T_c versus c/a (figure 7). It is found that T_c decreases with decreasing c/a, and T_c almost drops to zero when c/a = 1.0. These two results indicate a possible way to enhance T_c of MgB₂ by changing the lattice parameters or in-plane B–B bond length chemical means.

4. Conclusion

The potentials for simulation of MgB₂ were developed. With these potentials, we calculated the lattice parameters and volume dependence of pressure up to 240 GPa. The calculated results are in excellent agreement with the experimental results below 40 GPa and are reasonable predictions for the tendencies from 40 to 240 GPa. Our calculations show that the structure of MgB₂ changed from the AlB₂-type structure to the UHg₂-type structure with increasing pressure, and three phase transition points were found at high pressure. We analyse the effect of pressure on T_c by employing the McMillan expression with our calculated structural parameters. It is found that dT_c/dP is governed by the lattice stiffening and does not heavily

depend on the density of electronic states at the Fermi level. Using our calculated Grüneisen parameter $\gamma_{\rm G}$, our calculated $T_{\rm c}$ dependence of pressure agrees well with the experiments below 40 GPa. Our result predicts that the $T_{\rm c}$ of MgB₂ can be destroyed at about 90 GPa.

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